

CLASS NOTES

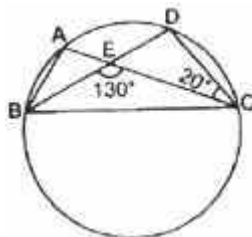
Class: IX

Topic: Circles
EX.10.5

Subject: MATHEMATICS

Q.5 In the figure, A, B, C and D are four points on a circle. AC and BD intersect at a point E such that $\angle BEC = 130^\circ$ and $\angle ECD = 20^\circ$.

Find $\angle BAC$.



Solution: In $\triangle CDE$,

Exterior $\angle BEC = \{\text{Sum of interior opposite angles}\}$

[BD is a straight line.]

$$130^\circ = \angle EDC + \angle ECD$$

$$130^\circ = \angle EDC + 20^\circ$$

$$\Rightarrow \angle EDC = 130^\circ - 20^\circ = 110^\circ$$

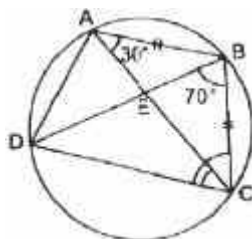
$$\Rightarrow \angle BDC = 110^\circ$$

Since, angles in the same segment are equal.

$$\angle BAC = \angle BDC$$

$$\Rightarrow \angle BAC = 110^\circ$$

Q.6 ABCD is a cyclic quadrilateral whose diagonals intersect at a point E. If $\angle DBC = 70^\circ$, $\angle BAC$ is 30° , find $\angle BCD$. Further, if $AB = BC$, find $\angle ECD$.



Solution: $\angle BAC = \angle BDC$

$$\Rightarrow 30^\circ = \angle BDC$$

$$\angle DBC = 70^\circ \text{ (given)}$$

In $\triangle BCD$

$$\angle BCD + \angle DBC + \angle CDB = 180^\circ \text{ (ASP)}$$

$$\Rightarrow \angle BCD + 70^\circ + 30^\circ = 180^\circ$$

$$\Rightarrow \angle BCD = 180^\circ - 70^\circ - 30^\circ = 80^\circ$$

Now, in $\triangle ABC$,

$$AB = BC$$

$$\Rightarrow \angle BCA = \angle BAC$$

$$\Rightarrow \angle BCA = 30^\circ$$

Now, $\angle BCA = \angle ECD = \angle BCD$

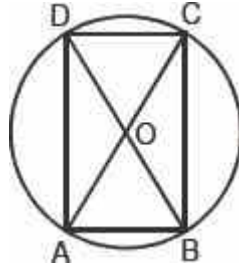
$$\Rightarrow 30^\circ + \angle ECD = 80^\circ$$

$$\Rightarrow \angle ECD = 80^\circ - 30^\circ = 50^\circ$$

[Angles opposite to equal sides of a triangle are equal]

Q.7 If diagonals of a cyclic quadrilateral are diameters of the circle through the vertices of the quadrilateral, prove that it is a rectangle.

Solution:



AC and BD are diameters.

$$\therefore AC = BD$$

Since a diameter divides a circle into equal parts.

$$\angle ABC = 90^\circ$$

$$\angle BCD = 90^\circ$$

and $\angle CDA = 90^\circ$

Now, in right $\triangle ABC$ and right $\triangle BAD$,

$$AC = BD$$

$$AB = AB$$

$$\therefore \triangle ABC \cong \triangle BAD$$

$$\Rightarrow BC = AD$$

Similarly, $AB = CD$

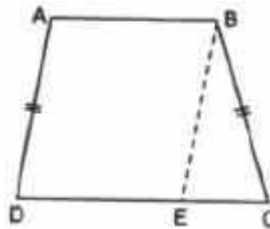
Thus, the cyclic quadrilateral ABCD is such that its opposite sides are equal and each of its angle is right angle.

[From (1)]
[Common]
[RHS criterion]
[c.p.c.t.]

Q.8 If the nonparallel sides of a trapezium are equal, prove that it is cyclic.

Solution: We have a trapezium ABCD such that $AB \parallel CD$ and $AD = BC$.

Let us draw $BE \parallel AD$ such that ABED is a parallelogram.



\therefore The opposite angles of a parallelogram are equal.

$$\therefore \angle BAD = \angle BED$$

and $AD = BE$

But $AD = BC$

\therefore From (2) and (3), we have

$$BE = BC$$

$$\Rightarrow \angle BEC = \angle BCE$$

are equal] ... (4)

$$\text{Now, } \angle BED + \angle BEC = 180^\circ$$

$$\Rightarrow \angle BAD + \angle BCE = 180^\circ$$

i.e., A pair of opposite angles of quadrilateral ABCD is 180° .

\therefore ABCD is cyclic.

\Rightarrow The trapezium ABCD is a cyclic.

... (1)
[Opposite sides of a parallelogram] ... (2)
[Given] ... (3)

[Angles opposite to equal sides of a triangle \triangle

[Linear pairs]
[Using (1) and (4)]

ASSIGNMENT : PRACTICE SIMILAR SUMS FROM R.S.AGRAWAL.

NOTE: THE STUDENTS ARE ADVISED TO WRITE THIS CONTENT IN THEIR MATHS FAIR NOTEBOOK.

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