

CLASS NOTES

Class: VIII

Topic: Ch.11 Mensuration

“This content is prepared absolutely from home.”

Subject: Mathematics

Ex.11.3

Soln.1(a) Length of cuboidal box (l) = 60 cm

Breadth of cuboidal box (b) = 40 cm

Height of cuboidal box (h) = 50 cm

∴ Total surface area of cuboidal box

$$= 2(lb + bh + hl)$$

$$= 2(60 \times 40 + 40 \times 50 + 50 \times 60)$$

$$= 2(2400 + 2000 + 3000)$$

$$= 2 \times 7400 = 14800 \text{ cm}^2$$

(b) Total surface area of cube (b) = $6(50)^2$

$$= 15000 \text{ cm}^2$$

Thus, the cuboidal box(a) will require lesser amount of material.

Ex.11.4

Soln.3 Area of base = $lb = 180 \text{ cm}^2$

$$V = 900 \text{ cm}^3$$

Volume of the cuboid = $l \times b \times h$

$$900 = 180 \times h$$

$$h = 5 \text{ cm}$$

Hence, the required height = 5 cm.

Soln.4 Volume of the cuboid

$$= l \times b \times h = 60 \text{ cm} \times 54 \text{ cm} \times 30 \text{ cm} = 97200 \text{ cm}^3$$

$$\text{Volume of the cube} = (\text{Side})^3 = (6)^3 = 216 \text{ cm}^3$$

Number of the cubes from the cuboid

$$= \frac{\text{Volume of the cuboid}}{\text{Volume of cube}}$$

$$= \frac{97200}{216}$$

$$= 450$$

Soln.2 Measurement of the suitcase

$$= 80 \text{ cm} \times 48 \text{ cm} \times 24 \text{ cm}$$

$$l = 80 \text{ cm}, b = 48 \text{ cm} \text{ and } h = 24 \text{ cm}$$

Total surface area of the suitcase

$$= 2[lb + bh + hl]$$

$$= 2[80 \times 48 + 48 \times 24 + 24 \times 80]$$

$$= 2[3840 + 1152 + 1920]$$

$$= 2 \times 6912$$

$$= 13824 \text{ cm}^2$$

Area of tarpaulin = length \times breadth = $l \times 96 \text{ cm}^2$

Area of tarpaulin = Area of 100 suitcase

$$96 \times l = 100 \times 13824$$

$$l = 100 \times 144 = 14400 \text{ cm} = 144 \text{ m}$$

Hence, the required length of the cloth = 144m.

Soln.5

$$V = 1.54 \text{ m}^3, d = 140 \text{ cm} = 1.40 \text{ m}$$

Volume of the cylinder = $\pi r^2 h$

$$1.54 = \frac{22}{7} \times \frac{1.4}{2} \times \frac{1.4}{2} \times h$$

$$\Rightarrow h = \frac{1.54 \times 7 \times 2 \times 2}{22 \times 1.4 \times 1.4}$$

$$= \frac{154 \cancel{14}^7 \times 7 \times 2 \times 2}{22 \cancel{2} \times 14 \cancel{2} \times 14 \cancel{2}}$$

$$= 1 \text{ m}$$

Hence, the height of cylinder = 1 m.

Soln.4 $l = 2 \text{ m}, b = 1.5 \text{ m}, h = 1 \text{ m}$

Area of the surface to be painted

= Total surface area of box – Area of base of box

$$= 2[lb + bh + hl] - lb$$

$$= 2[2 \times 1.5 + 1.5 \times 1 + 1 \times 2] - 2 \times 1$$

$$= 2[3 + 1.5 + 2] - 2$$

$$= 2[6.5] - 2$$

$$= 13 - 2$$

$$= 11 \text{ m}^2$$

Hence, the required area = 11 m^2 .

Soln6.

Here, $r = 1.5 \text{ m}$

$h = 7 \text{ m}$

∴ Volume of the milk tank = $\pi r^2 h$

$$= 227 \times 1.5 \times 1.5 \times 7$$

$$= 22 \times 2.25$$

$$= 49.50 \text{ m}^3$$

Volume of milk in litres = $49.50 \times 1000 \text{ L}$ ($\because 1 \text{ m}^3 = 1000$ litres)

$$= 49500 \text{ L}$$

Soln.5 Surface area of a cuboidal hall without bottom

$$\begin{aligned}
 &= \text{Total surface area} - \text{Area of base} \\
 &= 2 [lb + bh + hl] - lb \\
 &= 2 [15 \times 10 + 10 \times 7 + 7 \times 15] - 15 \times 10 \\
 &= 2[150 + 70 + 105] - 150 \\
 &= 2 [325] - 150 \\
 &= 650 - 150 \\
 &= 500 \text{ m}^2
 \end{aligned}$$

Area of the paint in one can = 100 m^2
 Number of cans required = $\frac{500}{100} = 5$ cans.

Soln.8 Width of the rectangular sheet
 = Circumference of the cylinder

$$\begin{aligned}
 33 &= 2\pi r \\
 \Rightarrow 33 &= 2 \times \frac{22}{7} \times r \\
 \Rightarrow r &= \frac{33^3 \times 7}{2 \times 22^2} = \frac{21}{4} \text{ cm}
 \end{aligned}$$

Now lateral surface area of the cylinder = $2\pi rh$

$$\begin{aligned}
 4224 &= 2 \times \frac{22}{7} \times \frac{21}{4} \times h \\
 \therefore h &= \frac{4224 \times 7 \times 4^2}{2 \times 22 \times 21} \\
 &= \frac{1408 \times 128}{11 \times 3}
 \end{aligned}$$

$h = 128 \text{ cm}$
 $l = 128 \text{ cm}, b = 33 \text{ cm}$
 Perimeter of the sheet = $2(l + b)$
 $= 2(128 + 33) = 2 \times 161 = 322 \text{ cm}$
 Hence, the required perimeter = 322 cm .

Soln.9 The lateral surface area of the road roller = $2\pi rh$

$$\begin{aligned}
 &= 2 \times \frac{22}{7} \times 42 \times 100 \\
 &\quad \left[\because r = \frac{84}{2} = 42 \text{ cm} \right] \\
 &= 26400 \text{ cm}^2
 \end{aligned}$$

Area covered by the roller in 750 complete revolutions

$$\begin{aligned}
 &= 26400 \times 750 \text{ cm}^2 \\
 &= 19800000 \text{ cm}^2 \\
 &= \frac{19800000}{10000} \text{ m}^2 \\
 &= 1980 \text{ m}^2
 \end{aligned}$$

Hence, the area of road = 1980 m^2

Soln.10 Here, $r = 14/2 = 7 \text{ cm}$

Height of the cylindrical label

$$= 20 - (2 + 2) = 16 \text{ cm}$$

Surface area of the cylindrical shaped label = $2\pi rh$

$$= 2 \times 22 \times 7 \times 16$$

$$= 704 \text{ cm}^2$$

Hence, the required area of label

$$= 704 \text{ cm}^2.$$

Soln.2 Cylinder B has a greater volume.

Verification:

Volume of cylinder A = $\pi r^2 h$

$$\begin{aligned}
 &= \frac{22^{11}}{7} \times \frac{7}{2} \times \frac{7}{2} \times 14^7 \\
 &= 539 \text{ cm}^3
 \end{aligned}$$

Volume of cylinder B = $\pi r^2 h$

$$\begin{aligned}
 &= \frac{22}{7} \times 7 \times 7 \times 7 \\
 &= 22 \times 49 = 1078 \text{ cm}^3
 \end{aligned}$$

Hence, volume of cylinder B is double to that of cylinder A. Hence verified.

Total surface area of cylinder A

$$\begin{aligned}
 &= 2\pi r(h + r) \\
 &= 2 \times \frac{22}{7} \times \frac{7}{2} \left(\frac{7}{2} + 14 \right) \\
 &= 2 \times \frac{22^{11}}{7} \times \frac{7}{2} \times \frac{35}{2} \\
 &= 385 \text{ cm}^2
 \end{aligned}$$

Total surface area of cylinder B

$$\begin{aligned}
 &= 2\pi r(h + r) \\
 &= 2 \times \frac{22}{7} \times 7(7 + 7) \\
 &= 2 \times \frac{22}{7} \times 7 \times 14 \\
 &= 616 \text{ cm}^2
 \end{aligned}$$

Hence, cylinder B has greater surface area.

Soln.7 Let the edge of the cube = $x \text{ cm}$

If the edge is doubled, then the new edge = $2x \text{ cm}$

(i) Original surface area = $6x^2 \text{ cm}^2$

New surface area = $6(2x)^2 = 6 \times 4x^2 = 24x^2$

Ratio = $6x^2 : 24x^2 = 1 : 4$

Hence, the new surface area will be four times the original surface area.

(ii) Original volume of the cube = $x^3 \text{ cm}^3$

New volume of the cube = $(2x)^3 = 8x^3 \text{ cm}^3$

Ratio = $x^3 : 8x^3 = 1 : 8$

Hence, the new volume will be eight times the original.

Soln.8 Volume of the reservoir = $108 \text{ m}^3 = 108000 \text{ L}$

[$\because 1 \text{ m}^3 = 1000 \text{ L}$]

Volume of water flowing into the reservoir in 1 minute = 60

$$= \frac{\text{Volume of the reservoir}}{\text{Rate of flowing the water}}$$

$$= \frac{108000}{60} \text{ minutes}$$

$$= 1800 \text{ minutes or } \frac{1800}{60} \text{ hours}$$

$$= 30 \text{ hours}$$

Time taken to fill the reservoir

Hence, the required hour to fill the reservoir = 30 hours

Assignment: Write the solutions and solve Q.3, 6 & 7 of Ex. 11.3, Q1 of Ex.11.4 neatly in fair copy.

