

## APPLIED MATHEMATICS (SET-1)

### Chapters (1. Numbers, Quantifications and Numerical Applications, 2. Differentiation and its Applications)

#### 1. Numbers, Quantifications and Numerical Applications

1.  $(8 \times 14)$  in 12 hours clock is

- (a) 4 O'clock      (b) 8 O'clock      (c) 6 O'clock      (d) 2 O'clock

2.  $(09:30+16:40)$  in 24 hours clock is

- (a) 03:10      (b) 26:10      (c) 2:10      (d) 25:70

3. If  $x \equiv 4 \pmod{7}$ , then positive values of  $x$  are

- (a) (4, 11, 18,...)      (b) (11, 18, 25,...)      (c) (4, 8, 12,...)      (d) (1, 8, 15, ...)

4.  $\sigma(15)$  is equal to

- (a) 8      (b) 24      (c) 4      (d) 16

5.  $\omega(32)$  is equal to

- (a) 1      (b) 3      (c) 5      (d) 7

6. Three types of wheat costing ₹18 per kg, ₹ 20 per kg and ₹25 per kg are mixed together. If the mixed variety is sold at ₹ 22 per kg, then the ratio in which these types of wheat should be mixed respectively is

- (a) 1:2:3      (b) 2:2:3      (c) 2:3:1      (d) 1:1:2

7. In what ratio must a grocer mix two varieties of pulses costing ₹85 per kg and ₹100 per kg respectively so as to get a mixture worth Rs 92 per kg?

- (a) 7:8      (b) 8:7      (c) 5:7      (d) 7:5

8. In what ratio must water be mixed with milk to gain  $16\frac{2}{3}\%$  on selling the mixture at cost price?

- (a) 1:6      (b) 6:1      (c) 3:2      (d) 2:3

9. Milk and water in two vessels A and B are in the ratio 5:3 and 5:4 respectively. In what ratio. the liquid of both the vessels be mixed to obtain a new mixture in which ratio of milk and water is 7:5 respectively?

- (a) 3:2      (b) 3:5      (c) 2:3      (d) 2:5

10. A boy's speed with the current is 15 km/h and the speed of the current is 2.5 km/h. The boy's speed against the current is

- (a) 8.5 km/h      (b) 9 km/h      (c) 10 km/h      (d) 12.5 km/h

11. A boat running downstream covers a distance of 16 km in 2 hours while for covering the same distance upstream it takes 4 hours. What is the speed of the boat in still water?

- (a) 4 km/h      (b) 6 km/h      (c) 8 km/h      (d) 10 km/h

12. The speed of a boat in still water is 15 km/h and the rate of current is 3 km/h. The distance travelled by boat downstream in 12 minutes is

- (a) 1.2 km      (b) 1.8 km.      (c) 2.4 km      (d) 3.6 km

13. A and B invest ₹ 50000 and ₹45000 respectively in a business. After 9 months B withdrew his investment. At the end of a year they earned a profit of ₹ 13400. What was B's share of profit?

- (a) ₹5400      (b) ₹ 3 9045      (c) ₹ 4500      (d) ₹ 5990

14. Nisha started a business with 540000. After few months Kusum joined her with an investment of Rs720000. If at the end of a year they shared the profit equally, then find after how many months Kusum joined Nisha?

- (a) 3      (b) 6      (c) 9      (d) 10

15. A, B and C started a business by investing money in the ratio 5: 7: 9. After 4 months D joined them by investing money equal to the investment of B. Find the ratio of their profits at the end of a year.

- (a) 15:17:28:25      (b) 15:21:27:14      (c) 12:15:17:9      (d) 12:17:19:13

### CASE STUDY

For completing a particular type of embroidery work, 2 women and 5 men take 4 days. Also, the same work was completed in 3 days by 3 women and 6 men.

Based on the above information, answer the following questions:

16. How much time was taken by 1 woman alone to finish the work?

- (a) 15 days      (b) 17 days      (c) 18 days      (d) 20 days

17. How much time was taken by 1 man alone to finish the work?

- (a) 35 days            (b) 36 days            (c) 37 days            (d) 38 days

18. In how many days will 2 women complete the same work?

- (a) 8 days            (b) 9 days            (c) 10 days            (d) 11 days

19. If the work is completed in 12 days, then find the number of men employed for the same.

- (a) 3 men            (b) 4 men            (c) 5 men            (d) 2 men


20. Find the ratio of efficiency of 1 woman to that of 1 man.

- (a) 1:2            (b) 2:1)            (c) 2:3            (d) 3:2

**2. Differentiation and its Applications.**

1	<p>Given that <math>x = at^2</math> and <math>y = 2at</math>, then value of <math>\frac{d^2y}{dx^2}</math> is</p> <p>(a) <math>-\frac{1}{2at^3}</math>            (b) <math>-\frac{1}{2at^2}</math>            (c) <math>\frac{1}{t^2}</math>            (d) <math>-\frac{2a}{t}</math></p>				
2	<p>If <math>e^x + e^y = e^{x+y}</math>, then <math>\frac{dy}{dx}</math> is:</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <tr> <td style="padding: 5px;">a) <math>e^{y-x}</math></td> <td style="padding: 5px;">b) <math>e^{x+y}</math></td> </tr> <tr> <td style="padding: 5px;">c) <math>-e^{y-x}</math></td> <td style="padding: 5px;">d) <math>2e^{x-y}</math></td> </tr> </table>	a) $e^{y-x}$	b) $e^{x+y}$	c) $-e^{y-x}$	d) $2e^{x-y}$
a) $e^{y-x}$	b) $e^{x+y}$				
c) $-e^{y-x}$	d) $2e^{x-y}$				
3	<p>If <math>x\sqrt{1+y} + y\sqrt{1+x} = 0</math>, The value of <math>(1+x^2) \frac{dy}{dx}</math> is equal to:</p> <p>a. 0            b. 1            c. -1            d. 2</p>				
4	<p>Find <math>dy/dx</math>; if <math>y = t \log t</math> and <math>x = (\log t)</math></p> <p>a. t            b. 1/t            c. <math>(1 + \log t)/t</math>            d. <math>(1 + \log t)t</math></p>				
5	<p>For what values of x is the rate of increase of total cost function <math>C(x) = x^3 - 5x^2 + 5x + 8</math> is twice the rate of increase of x?</p> <p>a. 3            b. 1, 3            c. 1/3            d. 3, 1/3</p>				
6	<p>If <math>y = \log(x + \sqrt{a^2 + x^2})</math>, Then the value of <math>(a^2 + x^2)y_2 + xy_1</math> is:</p> <p>a. 0            b. 1            c. x            d. -1</p>				

7	<p>The point at which the normal to the curve <math>y = x + \frac{1}{x}</math>, <math>x &gt; 0</math> is perpendicular to the line <math>3x - 4y - 7 = 0</math> is:</p> <table border="1" data-bbox="337 289 1133 359"> <tbody> <tr> <td>a) <math>(2, 5/2)</math></td> <td>b) <math>(\pm 2, 5/2)</math></td> </tr> <tr> <td>c) <math>(-1/2, 5/2)</math></td> <td>d) <math>(1/2, 5/2)</math></td> </tr> </tbody> </table>	a) $(2, 5/2)$	b) $(\pm 2, 5/2)$	c) $(-1/2, 5/2)$	d) $(1/2, 5/2)$	
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c) $(-1/2, 5/2)$	d) $(1/2, 5/2)$					
8	<p>The points on the curve <math>\frac{x^2}{9} + \frac{y^2}{16} = 1</math> at which the tangents are parallel to y-axis are:</p> <table border="1" data-bbox="337 470 1157 537"> <tbody> <tr> <td>a) <math>(0, \pm 4)</math></td> <td>b) <math>(\pm 4, 0)</math></td> </tr> <tr> <td>c) <math>(\pm 3, 0)</math></td> <td>d) <math>(0, \pm 3)</math></td> </tr> </tbody> </table>	a) $(0, \pm 4)$	b) $(\pm 4, 0)$	c) $(\pm 3, 0)$	d) $(0, \pm 3)$	
a) $(0, \pm 4)$	b) $(\pm 4, 0)$					
c) $(\pm 3, 0)$	d) $(0, \pm 3)$					
9	<p>The point(s) on the curve <math>y = x^3 - 11x + 5</math> at which the tangent is <math>y = x - 11</math> is/are:</p> <table border="1" data-bbox="337 632 1143 699"> <tbody> <tr> <td>a) <math>(-2, 19)</math></td> <td>b) <math>(2, -9)</math></td> </tr> <tr> <td>c) <math>(\pm 2, 19)</math></td> <td>d) <math>(-2, 19)</math> and <math>(2, -9)</math></td> </tr> </tbody> </table>	a) $(-2, 19)$	b) $(2, -9)$	c) $(\pm 2, 19)$	d) $(-2, 19)$ and $(2, -9)$	
a) $(-2, 19)$	b) $(2, -9)$					
c) $(\pm 2, 19)$	d) $(-2, 19)$ and $(2, -9)$					
10	<p>For which value of <math>m</math> is the line <math>y = mx + 1</math> a tangent to the curve <math>y^2 = 4x</math>?</p> <table border="1" data-bbox="337 772 1002 909"> <tbody> <tr> <td>a) <math>\frac{1}{2}</math></td> <td>b) 1</td> </tr> <tr> <td>c) 2</td> <td>d) 3</td> </tr> </tbody> </table>	a) $\frac{1}{2}$	b) 1	c) 2	d) 3	
a) $\frac{1}{2}$	b) 1					
c) 2	d) 3					
11	<p>The equation of tangent to the curve <math>y = x^3 + x</math> at the point <math>(1, 2)</math> is  (a) <math>4x + y = 6</math> (b) <math>4x - y = 2</math> (c) <math>4x - y = 12</math> (d) <math>4x + 3y = 7</math></p>					
12	<p>The intervals in which the function <math>f</math> given by <math>f(x) = x^2 - 4x + 6</math> is strictly increasing</p> <table border="1" data-bbox="337 1199 1295 1283"> <tbody> <tr> <td>a) <math>(-\infty, 2) \cup (2, \infty)</math></td> <td>b) <math>(2, \infty)</math></td> </tr> <tr> <td>c) <math>(-\infty, 2)</math></td> <td>d) <math>(-\infty, 2] \cup (2, \infty)</math></td> </tr> </tbody> </table>	a) $(-\infty, 2) \cup (2, \infty)$	b) $(2, \infty)$	c) $(-\infty, 2)$	d) $(-\infty, 2] \cup (2, \infty)$	
a) $(-\infty, 2) \cup (2, \infty)$	b) $(2, \infty)$					
c) $(-\infty, 2)$	d) $(-\infty, 2] \cup (2, \infty)$					
13	<p>The real function <math>f(x) = 2x^3 - 3x^2 - 36x + 7</math> is:</p> <table border="1" data-bbox="337 1360 1268 1650"> <tbody> <tr> <td>a) Strictly increasing in <math>(-\infty, -2)</math> and strictly decreasing in <math>(-2, \infty)</math></td> </tr> <tr> <td>b) Strictly decreasing in <math>(-2, 3)</math></td> </tr> <tr> <td>c) Strictly decreasing in <math>(-\infty, 3)</math> and strictly increasing in <math>(3, \infty)</math></td> </tr> <tr> <td>d) Strictly decreasing in <math>(-\infty, -2) \cup (3, \infty)</math></td> </tr> </tbody> </table>	a) Strictly increasing in $(-\infty, -2)$ and strictly decreasing in $(-2, \infty)$	b) Strictly decreasing in $(-2, 3)$	c) Strictly decreasing in $(-\infty, 3)$ and strictly increasing in $(3, \infty)$	d) Strictly decreasing in $(-\infty, -2) \cup (3, \infty)$	
a) Strictly increasing in $(-\infty, -2)$ and strictly decreasing in $(-2, \infty)$						
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c) Strictly decreasing in $(-\infty, 3)$ and strictly increasing in $(3, \infty)$						
d) Strictly decreasing in $(-\infty, -2) \cup (3, \infty)$						
14	<p>The value of <math>b</math> for which the function <math>f(x) = x + \cos x + b</math> is strictly decreasing over <math>\mathbf{R}</math> is:</p> <table border="1" data-bbox="337 1717 1279 1795"> <tbody> <tr> <td>a) <math>b &lt; 1</math></td> <td>b) No value of <math>b</math> exists</td> </tr> <tr> <td>c) <math>b \leq 1</math></td> <td>d) <math>b \geq 1</math></td> </tr> </tbody> </table>	a) $b < 1$	b) No value of $b$ exists	c) $b \leq 1$	d) $b \geq 1$	
a) $b < 1$	b) No value of $b$ exists					
c) $b \leq 1$	d) $b \geq 1$					

15	<p>The function <math>y = \frac{1}{x}</math> is strictly decreasing in the interval(s)</p> <p>(a) <math>(0, \infty)</math> only (b) <math>(-\infty, 0)</math> only (c) <math>(-\infty, 0)</math> as well as <math>(0, \infty)</math> (d) <math>\mathbf{R}</math></p>					
16	<p>The total cost function is given by <math>C(x) = x^2 + 30x + 1500</math>. The marginal cost when 10 units are produced is:</p> <p>(a) ₹ 20 (b) ₹ 30 (c) ₹ 50 (d) ₹ 70</p>					
17	<p>The demand function of a toy is, <math>x = 75 - 3p</math> and its total cost function is <math>TC = 100 + 3x</math>. For maximum profit the value of <math>x</math> is</p> <p>(a) 33 (b) 31 (c) 29 (d) 24</p>					
18	<p>The variable cost of producing <math>x</math> units is <math>V(x) = x^2 + 2x</math>. If the company incurs a fixed cost of ₹10,000, then the level of output where the average cost is minimum is</p> <p>(a) 10 units (b) 50 units (c) 100 units (d) 200 units</p>					
19	<p>The least value of the function <math>f(x) = 2\cos x + x</math> in the closed interval <math>[0, \frac{\pi}{2}]</math> is:</p> <table border="1" data-bbox="337 821 1101 921"> <tbody> <tr> <td data-bbox="337 821 716 863">a) 2</td> <td data-bbox="716 821 1101 863">b) <math>\frac{\pi}{6} + \sqrt{3}</math></td> </tr> <tr> <td data-bbox="337 863 716 921">c) <math>\frac{\pi}{2}</math></td> <td data-bbox="716 863 1101 921">d) The least value does not exist.</td> </tr> </tbody> </table>	a) 2	b) $\frac{\pi}{6} + \sqrt{3}$	c) $\frac{\pi}{2}$	d) The least value does not exist.	
a) 2	b) $\frac{\pi}{6} + \sqrt{3}$					
c) $\frac{\pi}{2}$	d) The least value does not exist.					
20	<p>The area of a trapezium is defined by function <math>f</math> and given by <math>f(x) = (10 + x)\sqrt{100 - x^2}</math>, then the area when it is maximised is:</p> <table border="1" data-bbox="337 1037 1101 1121"> <tbody> <tr> <td data-bbox="337 1037 716 1079">a) <math>75\text{cm}^2</math></td> <td data-bbox="716 1037 1101 1079">b) <math>7\sqrt{3}\text{cm}^2</math></td> </tr> <tr> <td data-bbox="337 1079 716 1121">c) <math>75\sqrt{3}\text{cm}^2</math></td> <td data-bbox="716 1079 1101 1121">d) <math>5\text{cm}^2</math></td> </tr> </tbody> </table>	a) $75\text{cm}^2$	b) $7\sqrt{3}\text{cm}^2$	c) $75\sqrt{3}\text{cm}^2$	d) $5\text{cm}^2$	
a) $75\text{cm}^2$	b) $7\sqrt{3}\text{cm}^2$					
c) $75\sqrt{3}\text{cm}^2$	d) $5\text{cm}^2$					
	<p style="text-align: center;"><b><u>CASE STUDY</u></b></p> <div style="display: flex; align-items: flex-start;">  <div> <p>The fuel cost per hour for running a train is proportional to the square of the speed it generates in km per hour. If the fuel costs ₹ 48 per hour at speed 16 km per hour and the fixed charges to run the train amount to ₹ 1200 per hour.</p> <p>Assume the speed of the train as <math>v</math> km/h.</p> </div> </div>					
	<p><b>Based on the given information, answer the following questions.</b></p>					
21	<p>Given that the fuel cost per hour is <math>k</math> times the square of the speed the train generates in km/h, the value of <math>k</math> is:</p> <table border="1" data-bbox="337 1724 1166 1837"> <tbody> <tr> <td data-bbox="337 1724 751 1776">a) <math>\frac{16}{3}</math></td> <td data-bbox="751 1724 1166 1776">b) <math>\frac{1}{3}</math></td> </tr> <tr> <td data-bbox="337 1776 751 1837">c) 3</td> <td data-bbox="751 1776 1166 1837">d) <math>\frac{3}{16}</math></td> </tr> </tbody> </table>	a) $\frac{16}{3}$	b) $\frac{1}{3}$	c) 3	d) $\frac{3}{16}$	
a) $\frac{16}{3}$	b) $\frac{1}{3}$					
c) 3	d) $\frac{3}{16}$					

22	<p>If the train has travelled a distance of 500km, then the total cost of running the train is given by function:</p> <table border="1" data-bbox="337 285 1162 472"> <tr> <td data-bbox="337 285 748 380">a) <math>\frac{15}{16}v + \frac{600000}{v}</math></td> <td data-bbox="748 285 1162 380">b) <math>\frac{375}{4}v + \frac{600000}{v}</math></td> </tr> <tr> <td data-bbox="337 380 748 472">c) <math>\frac{5}{16}v^2 + \frac{150000}{v}</math></td> <td data-bbox="748 380 1162 472">d) <math>\frac{3}{16}v + \frac{6000}{v}</math></td> </tr> </table>	a) $\frac{15}{16}v + \frac{600000}{v}$	b) $\frac{375}{4}v + \frac{600000}{v}$	c) $\frac{5}{16}v^2 + \frac{150000}{v}$	d) $\frac{3}{16}v + \frac{6000}{v}$		
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c) $\frac{5}{16}v^2 + \frac{150000}{v}$	d) $\frac{3}{16}v + \frac{6000}{v}$						
23	<p>The most economical speed to run the train is:</p> <table border="1" data-bbox="337 543 1162 632"> <tr> <td data-bbox="337 543 748 590">a) 18km/h</td> <td data-bbox="748 543 1162 590">b) 5km/h</td> </tr> <tr> <td data-bbox="337 590 748 632">c) 80km/h</td> <td data-bbox="748 590 1162 632">d) 40km/h</td> </tr> </table>	a) 18km/h	b) 5km/h	c) 80km/h	d) 40km/h		
a) 18km/h	b) 5km/h						
c) 80km/h	d) 40km/h						
24	<p>The fuel cost for the train to travel 500km at the most economical speed is:</p> <table border="1" data-bbox="337 703 1050 791"> <tr> <td data-bbox="337 703 691 749">a) ₹ 3750</td> <td data-bbox="691 703 1050 749">b) ₹ 750</td> </tr> <tr> <td data-bbox="337 749 691 791">c) ₹ 7500</td> <td data-bbox="691 749 1050 791">d) ₹ 75000</td> </tr> </table>	a) ₹ 3750	b) ₹ 750	c) ₹ 7500	d) ₹ 75000		
a) ₹ 3750	b) ₹ 750						
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25	<p>The total cost of the train to travel 500km at the most economical speed is:</p> <table border="1" data-bbox="337 854 1050 940"> <tr> <td data-bbox="337 854 691 900">a) ₹ 3750</td> <td data-bbox="691 854 1050 900">b) ₹ 75000</td> </tr> <tr> <td data-bbox="337 900 691 940">c) ₹ 7500</td> <td data-bbox="691 900 1050 940">d) ₹ 15000</td> </tr> </table>	a) ₹ 3750	b) ₹ 75000	c) ₹ 7500	d) ₹ 15000		
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c) ₹ 7500	d) ₹ 15000						

**APPLIED MATHEMATICS :SET-2**

**Algebra ( Matrix) 25 Questions**

<b>1</b>	<p>If <math>A = \begin{bmatrix} 3 &amp; 4 \\ 2 &amp; 3 \end{bmatrix}</math>, <math>B = \begin{bmatrix} -2 &amp; -2 \\ 0 &amp; -1 \end{bmatrix}</math> then <math>(A+B)^{-1}</math> is:</p> <p>A <math>\begin{bmatrix} -1 &amp; 1 \\ 1 &amp; -1/2 \end{bmatrix}</math>                      B does not exist</p> <p>C is a skew-symmetric            D None of these</p>						
<b>2</b>	<p>In a <math>3 \times 3</math> matrix A, value of <math>a_{12}c_{13} + a_{22}c_{23} + a_{32}c_{33}</math>, where <math>c_{ij}</math> is the cofactor of <math>a_{ij}</math> is</p> <p>(a) 0                      (b) -1                      (c) 1                      (d)  A </p>						
<b>3</b>	<p>If A is a square matrix of order 3 and <math> A  = -2</math>, then <math> adj(A) </math> is equal to</p> <p>(a) -8                      (b) -2                      (c) 0                      (d) 4</p>						
<b>4</b>	<p>If two square matrices A and B are such that <math> AB  = 12</math> and <math> B  = -4</math>, then value of <math> A </math> is:</p> <p>(a) 8                      (b) -8                      (c) -3                      (d) 16</p>						
<b>5</b>	<p>Value of k, for which <math>A = \begin{bmatrix} k &amp; 8 \\ 4 &amp; 2k \end{bmatrix}</math> is a singular matrix is:</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <tbody> <tr> <td style="width: 50%; padding: 5px;">a) 4</td> <td style="width: 50%; padding: 5px;">b) -4</td> </tr> <tr> <td style="width: 50%; padding: 5px;">c) <math>\pm 4</math></td> <td style="width: 50%; padding: 5px;">d) 0</td> </tr> </tbody> </table>	a) 4	b) -4	c) $\pm 4$	d) 0		
a) 4	b) -4						
c) $\pm 4$	d) 0						
<b>6</b>	<p>Given that A is a square matrix of order 3 and <math> A  = -4</math>, then <math> adj A </math> is equal to:</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <tbody> <tr> <td style="width: 50%; padding: 5px;">a) -4</td> <td style="width: 50%; padding: 5px;">b) 4</td> </tr> <tr> <td style="width: 50%; padding: 5px;">c) -16</td> <td style="width: 50%; padding: 5px;">d) 16</td> </tr> </tbody> </table>	a) -4	b) 4	c) -16	d) 16		
a) -4	b) 4						
c) -16	d) 16						
<b>7</b>	<p>If <math>\begin{bmatrix} 2a + b &amp; a - 2b \\ 5c - d &amp; 4c + 3d \end{bmatrix} = \begin{bmatrix} 4 &amp; -3 \\ 11 &amp; 24 \end{bmatrix}</math>, then value of <math>a + b - c + 2d</math> is:</p> <table border="1" style="width: 100%; border-collapse: collapse;"> <tbody> <tr> <td style="width: 50%; padding: 5px;">a) 8</td> <td style="width: 50%; padding: 5px;">b) 10</td> </tr> <tr> <td style="width: 50%; padding: 5px;">c) 4</td> <td style="width: 50%; padding: 5px;">d) -8</td> </tr> </tbody> </table>	a) 8	b) 10	c) 4	d) -8		
a) 8	b) 10						
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8	<p>Given that matrices A and B are of order <math>3 \times n</math> and <math>m \times 5</math> respectively, then the order of matrix <math>C = 5A + 3B</math> is:</p> <table border="1" data-bbox="289 296 1133 369"> <tbody> <tr> <td>a) <math>3 \times 5</math> and <math>m = n</math></td> <td>b) <math>3 \times 5</math></td> </tr> <tr> <td>c) <math>3 \times 3</math></td> <td>d) <math>5 \times 5</math></td> </tr> </tbody> </table>	a) $3 \times 5$ and $m = n$	b) $3 \times 5$	c) $3 \times 3$	d) $5 \times 5$		
a) $3 \times 5$ and $m = n$	b) $3 \times 5$						
c) $3 \times 3$	d) $5 \times 5$						
9	<p>For matrix <math>A = \begin{bmatrix} 2 &amp; 5 \\ -11 &amp; 7 \end{bmatrix}</math>, <math>(adjA)'</math> is equal to:</p> <table border="1" data-bbox="289 485 1284 705"> <tbody> <tr> <td>a) <math>\begin{bmatrix} -2 &amp; -5 \\ 11 &amp; -7 \end{bmatrix}</math></td> <td>b) <math>\begin{bmatrix} 7 &amp; 5 \\ 11 &amp; 2 \end{bmatrix}</math></td> </tr> <tr> <td>c) <math>\begin{bmatrix} 7 &amp; 11 \\ -5 &amp; 2 \end{bmatrix}</math></td> <td>d) <math>\begin{bmatrix} 7 &amp; -5 \\ 11 &amp; 2 \end{bmatrix}</math></td> </tr> </tbody> </table>	a) $\begin{bmatrix} -2 & -5 \\ 11 & -7 \end{bmatrix}$	b) $\begin{bmatrix} 7 & 5 \\ 11 & 2 \end{bmatrix}$	c) $\begin{bmatrix} 7 & 11 \\ -5 & 2 \end{bmatrix}$	d) $\begin{bmatrix} 7 & -5 \\ 11 & 2 \end{bmatrix}$		
a) $\begin{bmatrix} -2 & -5 \\ 11 & -7 \end{bmatrix}$	b) $\begin{bmatrix} 7 & 5 \\ 11 & 2 \end{bmatrix}$						
c) $\begin{bmatrix} 7 & 11 \\ -5 & 2 \end{bmatrix}$	d) $\begin{bmatrix} 7 & -5 \\ 11 & 2 \end{bmatrix}$						
10	<p>Given that <math>A = [a_{ij}]</math> is a square matrix of order <math>3 \times 3</math> and <math> A  = -7</math>, then the value of <math>\sum_{i=1}^3 a_{i2}A_{i2}</math>, where <math>A_{ij}</math> denotes the cofactor of element <math>a_{ij}</math> is:</p> <table border="1" data-bbox="289 848 1284 921"> <tbody> <tr> <td>a) 7</td> <td>b) -7</td> </tr> <tr> <td>c) 0</td> <td>d) 49</td> </tr> </tbody> </table>	a) 7	b) -7	c) 0	d) 49		
a) 7	b) -7						
c) 0	d) 49						
11	<p>If matrix <math>A = \begin{pmatrix} a &amp; b &amp; -5 \\ c &amp; d &amp; 0 \\ 5 &amp; 0 &amp; 0 \end{pmatrix}</math> is skew symmetric, then value of <math>2a + b + c - 3d</math> is:</p> <p>(a) 1                      (b) -1                      (c) 0                      (d) 2</p>						
12	<p>In which of the technology matrix, Hawkins- Simon conditions are satisfied</p> <p>(a) <math>\begin{pmatrix} 0.2 &amp; 0.9 \\ 0.8 &amp; 0.1 \end{pmatrix}</math>                      (b) <math>\begin{pmatrix} 0.7 &amp; 0.3 \\ 0.2 &amp; 1.2 \end{pmatrix}</math></p> <p>(c) <math>\begin{pmatrix} 1.02 &amp; 0.5 \\ 0.6 &amp; 0.8 \end{pmatrix}</math>                      (d) <math>\begin{pmatrix} 0.3 &amp; 0.2 \\ 0.1 &amp; 0.5 \end{pmatrix}</math></p>						
13	<p>If <math>A = \begin{bmatrix} 0 &amp; 2 \\ 3 &amp; -4 \end{bmatrix}</math> and <math>kA = \begin{bmatrix} 0 &amp; 3a \\ 2b &amp; 24 \end{bmatrix}</math>, then the values of <math>k, a</math> and <math>b</math> respectively are:</p> <table border="1" data-bbox="289 1583 1292 1656"> <tbody> <tr> <td>a) -6, -12, -18</td> <td>b) -6, -4, -9</td> </tr> <tr> <td>c) -6, 4, 9</td> <td>d) -6, 12, 18</td> </tr> </tbody> </table>	a) -6, -12, -18	b) -6, -4, -9	c) -6, 4, 9	d) -6, 12, 18		
a) -6, -12, -18	b) -6, -4, -9						
c) -6, 4, 9	d) -6, 12, 18						



<p><b>14</b></p>	<p>If <math>A = [a_{ij}]</math> is a square matrix of order 2 such that <math>a_{ij} = \begin{cases} 1, &amp; \text{when } i \neq j \\ 0, &amp; \text{when } i = j \end{cases}</math>, then <math>A^2</math> is:</p> <table border="1" data-bbox="285 352 1114 537"> <tbody> <tr> <td>a) <math>\begin{bmatrix} 1 &amp; 0 \\ 1 &amp; 0 \end{bmatrix}</math></td> <td>b) <math>\begin{bmatrix} 1 &amp; 1 \\ 0 &amp; 0 \end{bmatrix}</math></td> </tr> <tr> <td>c) <math>\begin{bmatrix} 1 &amp; 1 \\ 1 &amp; 0 \end{bmatrix}</math></td> <td>d) <math>\begin{bmatrix} 1 &amp; 0 \\ 0 &amp; 1 \end{bmatrix}</math></td> </tr> </tbody> </table>	a) $\begin{bmatrix} 1 & 0 \\ 1 & 0 \end{bmatrix}$	b) $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$	c) $\begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$	d) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$		
a) $\begin{bmatrix} 1 & 0 \\ 1 & 0 \end{bmatrix}$	b) $\begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$						
c) $\begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$	d) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$						
<p><b>15</b></p>	<p>Given that <math>A</math> is a non-singular matrix of order 3 such that <math>A^2 = 2A</math>, then value of <math> 2A </math> is:</p> <table border="1" data-bbox="285 688 1289 764"> <tbody> <tr> <td>a) 4</td> <td>b) 8</td> </tr> <tr> <td>c) 64</td> <td>d) 16</td> </tr> </tbody> </table>	a) 4	b) 8	c) 64	d) 16		
a) 4	b) 8						
c) 64	d) 16						
<p><b>16</b></p>	<p>If <math>A</math> is square matrix such that <math>A^2 = A</math>, then <math>(I + A)^3 - 7A</math> is equal to:</p> <table border="1" data-bbox="285 890 1289 961"> <tbody> <tr> <td>a) <math>A</math></td> <td>b) <math>I + A</math></td> </tr> <tr> <td>c) <math>I - A</math></td> <td>d) <math>I</math></td> </tr> </tbody> </table>	a) $A$	b) $I + A$	c) $I - A$	d) $I$		
a) $A$	b) $I + A$						
c) $I - A$	d) $I$						
<p><b>17</b></p>	<p>For <math>A = \begin{bmatrix} 3 &amp; 1 \\ -1 &amp; 2 \end{bmatrix}</math>, then <math>14A^{-1}</math> is given by:</p> <table border="1" data-bbox="285 1108 1289 1297"> <tbody> <tr> <td>a) <math>14 \begin{bmatrix} 2 &amp; -1 \\ 1 &amp; 3 \end{bmatrix}</math></td> <td>b) <math>\begin{bmatrix} 4 &amp; -2 \\ 2 &amp; 6 \end{bmatrix}</math></td> </tr> <tr> <td>c) <math>2 \begin{bmatrix} 2 &amp; -1 \\ 1 &amp; -3 \end{bmatrix}</math></td> <td>d) <math>2 \begin{bmatrix} -3 &amp; -1 \\ 1 &amp; -2 \end{bmatrix}</math></td> </tr> </tbody> </table>	a) $14 \begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix}$	b) $\begin{bmatrix} 4 & -2 \\ 2 & 6 \end{bmatrix}$	c) $2 \begin{bmatrix} 2 & -1 \\ 1 & -3 \end{bmatrix}$	d) $2 \begin{bmatrix} -3 & -1 \\ 1 & -2 \end{bmatrix}$		
a) $14 \begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix}$	b) $\begin{bmatrix} 4 & -2 \\ 2 & 6 \end{bmatrix}$						
c) $2 \begin{bmatrix} 2 & -1 \\ 1 & -3 \end{bmatrix}$	d) $2 \begin{bmatrix} -3 & -1 \\ 1 & -2 \end{bmatrix}$						
<p><b>18</b></p>	<p>Given that <math>A = \begin{bmatrix} \alpha &amp; \beta \\ \gamma &amp; -\alpha \end{bmatrix}</math> and <math>A^2 = 3I</math>, then:</p> <table border="1" data-bbox="285 1457 1289 1533"> <tbody> <tr> <td>a) <math>1 + \alpha^2 + \beta\gamma = 0</math></td> <td>b) <math>1 - \alpha^2 - \beta\gamma = 0</math></td> </tr> <tr> <td>c) <math>3 - \alpha^2 - \beta\gamma = 0</math></td> <td>d) <math>3 + \alpha^2 + \beta\gamma = 0</math></td> </tr> </tbody> </table>	a) $1 + \alpha^2 + \beta\gamma = 0$	b) $1 - \alpha^2 - \beta\gamma = 0$	c) $3 - \alpha^2 - \beta\gamma = 0$	d) $3 + \alpha^2 + \beta\gamma = 0$		
a) $1 + \alpha^2 + \beta\gamma = 0$	b) $1 - \alpha^2 - \beta\gamma = 0$						
c) $3 - \alpha^2 - \beta\gamma = 0$	d) $3 + \alpha^2 + \beta\gamma = 0$						
<p><b>19</b></p>	<p>Let <math>A = \begin{bmatrix} 1 &amp; \sin\alpha &amp; 1 \\ -\sin\alpha &amp; 1 &amp; \sin\alpha \\ -1 &amp; -\sin\alpha &amp; 1 \end{bmatrix}</math>, where <math>0 \leq \alpha \leq 2\pi</math>, then:</p> <table border="1" data-bbox="285 1717 1289 1793"> <tbody> <tr> <td>a) <math> A =0</math></td> <td>b) <math> A  \in (2, \infty)</math></td> </tr> <tr> <td>c) <math> A  \in (2,4)</math></td> <td>d) <math> A  \in [2,4]</math></td> </tr> </tbody> </table>	a) $ A =0$	b) $ A  \in (2, \infty)$	c) $ A  \in (2,4)$	d) $ A  \in [2,4]$		
a) $ A =0$	b) $ A  \in (2, \infty)$						
c) $ A  \in (2,4)$	d) $ A  \in [2,4]$						

20

If  $A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & 4 \\ 0 & 1 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 2 & 2 & -4 \\ -4 & 2 & -4 \\ 2 & -1 & 5 \end{bmatrix}$ , then:

a) $A^{-1} = B$	b) $A^{-1} = 6B$
c) $B^{-1} = B$	d) $B^{-1} = \frac{1}{6}A$

### CASE STUDY

The economy of a state is composed of various sectors. To understand the basic concept, we consider two sectors coal mining (sector 1) and utilities (sector 2). The coal mining produces coal and utilities produces electricity. Assume that these products are measured by their rupee value. By one unit of product we mean 1 rupee worth of that product. To produce ₹1 worth of coal the coal mining sector uses ₹0.50 of coal and ₹0.10 of electricity. To produce ₹1 worth of electricity the utilities sector uses ₹0.25 of coal and ₹0.25 of electricity.



Based on the above information, answer the following questions:

21

The technology coefficient matrix A is

(a)  $\begin{pmatrix} 0.50 & 0.10 \\ 0.25 & 0.25 \end{pmatrix}$

(b)  $\begin{pmatrix} 0.50 & 0.25 \\ 0.10 & 0.25 \end{pmatrix}$

(c)  $\begin{pmatrix} 0.25 & 0.25 \\ 0.50 & 0.10 \end{pmatrix}$

(d)  $\begin{pmatrix} 0.10 & 0.50 \\ 0.25 & 0.25 \end{pmatrix}$

22	<p>The matrix <math>(I - A)^{-1}</math> is</p> <p>(a) <math>\frac{1}{8} \begin{pmatrix} 15 &amp; 5 \\ 2 &amp; 10 \end{pmatrix}</math>                      (b) <math>\frac{1}{7} \begin{pmatrix} 15 &amp; 2 \\ 5 &amp; 10 \end{pmatrix}</math></p> <p>(c) <math>\frac{1}{7} \begin{pmatrix} 15 &amp; 5 \\ 2 &amp; 10 \end{pmatrix}</math>                      (d) <math>\frac{20}{7} \begin{pmatrix} 0.75 &amp; 0.25 \\ 0.50 &amp; 0.10 \end{pmatrix}</math></p>		
23	<p>The system is viable because</p> <p>(a) <math> I - A  &gt; 0</math> and diagonal elements of <math>(I - A) &lt; 0</math></p> <p>(b) <math> I - A  &gt; 0</math> and diagonal elements of <math>(I - A) &gt; 0</math></p> <p>(c) <math> I - A  &lt; 0</math> and diagonal elements of <math>(I - A) &gt; 0</math></p> <p>(d) <math> I - A  &lt; 0</math> and diagonal elements of <math>(I - A) &lt; 0</math></p>		
24	<p>If there is external demand worth ₹7000 of coal and ₹14000 of electricity, then production of two sectors to meet the demand is</p> <p>(a) ₹ 25000 of coal, ₹ 22000 of electricity</p> <p>(b) ₹ 12000 of coal, ₹ 20000 of electricity</p> <p>(c) ₹ 15000 of coal, ₹ 22000 of electricity</p> <p>(d) ₹ 27000 of coal, ₹ 22000 of electricity</p>		
25	<p>How much worth of coal and electricity is used internally?</p> <p>(a) ₹ 25000 of coal, ₹22000 of electricity</p> <p>(b) ₹ 22000 of coal, ₹15000 of electricity</p> <p>(c) ₹ 20000 of coal, ₹10000 of electricity</p> <p>(d) ₹ 18000 of coal, ₹8000 of electricity</p>		
<b>Determinants</b>			
1	<p>If A(3 ,4) B(-7, 2) and C(x, y) are collinear then</p> <p>A) <math>x+5y+17 = 0</math>      B) <math>x+5y+13 = 0</math></p> <p>C) <math>x-5y+17 = 0</math>      D) None of these</p>		

2	<p>The value of determinant <math>\begin{vmatrix} 1 &amp; bc &amp; a(b+c) \\ 1 &amp; ca &amp; b(c+a) \\ 1 &amp; ab &amp; c(a+b) \end{vmatrix}</math> will be equal to</p> <p>A) <math>a^3+b^3+c^3</math>                      B) <math>3abc</math>  C) <math>a^3+b^3+c^3 -3abc</math>                      D) <math>0</math></p>		
3	<p>If <math>\begin{vmatrix} 2x &amp; -1 \\ 4 &amp; 2 \end{vmatrix} = \begin{vmatrix} 3 &amp; 0 \\ 2 &amp; 1 \end{vmatrix}</math> then <math>x</math> is</p> <p>A) <math>3</math>    B) <math>2/3</math>    C) <math>3/2</math>    D) <math>-1/4</math></p>		
4	<p>If <math>\Delta_1 = \begin{vmatrix} 1 &amp; 1 &amp; 1 \\ a &amp; b &amp; c \\ a^2 &amp; b^2 &amp; c^2 \end{vmatrix}</math>, <math>\Delta_2 = \begin{vmatrix} 1 &amp; bc &amp; a \\ 1 &amp; ca &amp; b \\ 1 &amp; ab &amp; c \end{vmatrix}</math> then:</p> <p>A) <math>\Delta_1 = \Delta_2</math>                                      B) <math>\Delta_1 + 3\Delta_2 = 0</math>  C) <math>\Delta_1 + \Delta_2 = 0</math>                                      D) <math>\Delta_1 + 2\Delta_2 = 0</math></p>		
5	<p>The value of <math>\begin{vmatrix} 5^2 &amp; 5^3 &amp; 5^4 \\ 5^3 &amp; 5^4 &amp; 5^5 \\ 5^4 &amp; 5^5 &amp; 5^6 \end{vmatrix}</math> is:</p> <p>A) <math>5^2</math>                      B) <math>0</math>                      C) <math>5^{13}</math>                      D) <math>5^6</math></p>		
6	<p><math>\begin{vmatrix} 1 &amp; bc &amp; a(b+c) \\ 1 &amp; ca &amp; b(c+a) \\ 1 &amp; ab &amp; c(a+b) \end{vmatrix}</math> will be equal to</p> <p>A <math>a^3+b^3+c^3</math>                                      B <math>3bc</math>  C <math>a^3+b^3+c^3 -3abc</math>                                      D <math>0</math></p>		

7	<p>Let <math>\Delta = \begin{vmatrix} Ax^2 &amp; x^3 &amp; 1 \\ By^2 &amp; y^3 &amp; 1 \\ Cz^2 &amp; z^3 &amp; 1 \end{vmatrix}</math> and</p> <p><math>\Delta_1 = \begin{vmatrix} Ax &amp; By &amp; Cz \\ x^2 &amp; y^2 &amp; z^2 \\ yz &amp; zx &amp; xy \end{vmatrix}</math>, then</p> <p>A <math>\Delta_1 + \Delta = 0</math>                      B <math>\Delta_1 \neq \Delta</math></p> <p>C <math>x \Delta_1 - \Delta = 0</math>                      D <math>\Delta_1 - \Delta = 0</math></p>		
8	<p><math>\Delta = \begin{vmatrix} \cos x &amp; -\sin x &amp; 1 \\ \sin x &amp; \cos x &amp; 1 \\ \cos(x+y) &amp; -\sin(x+y) &amp; 0 \end{vmatrix}</math>, lies</p> <p>in the interval</p> <p>A <math>[-\sqrt{2}, \sqrt{2}]</math>                      B <math>[-1, 1]</math></p> <p>C <math>[-\sqrt{2}, 1]</math>                      D <math>[-1, \sqrt{2}]</math></p>		
9	<p>If <math>\begin{vmatrix} 2x &amp; 5 \\ 8 &amp; x \end{vmatrix} = \begin{vmatrix} 6 &amp; 2 \\ 7 &amp; 3 \end{vmatrix}</math> then value of x is</p> <p>A <math>\pm\sqrt{22}</math>                      B 6                      C 3                      D <math>\pm\sqrt{3}</math></p>		
10	<p>If solving a system of linear equations in 3 variables by Cramer's rule, we get <math>\Delta = 0</math> and at least one of <math>\Delta_x, \Delta_y, \Delta_z</math> is non-zero then the system of linear equations has</p> <p>(a) no solution                      (b) unique solution</p> <p>(c) infinitely many solutions                      (d) trivial solution</p>		
11	<p>If the system of equations, <math>x + 2y - 3z = 1</math>, <math>(k + 3)z = 3</math>, <math>(2k + 1)x + z = 0</math> is inconsistent, then the value of k is</p> <p>(a) -3                      (b) <math>\frac{1}{2}</math>                      (c) 0                      (d) 2</p>		
12	<p>If the system of equations <math>x + ay = 0</math>, <math>az + y = 0</math> and <math>ax + z = 0</math> has infinite solutions, then the value of a is</p>		

	(a) $-1$ (b) $1$ (c) $0$ (d) No real values		
<b>13</b>	If the system of equations $x - ky - z = 0$ , $kx - y - z = 0$ and $x + y - z = 0$ has a non zero solution, then the possible value of $k$ are (a) $-1, 2$ (b) $1, 2$ (c) $0, 1$ (d) $-1, 1$		
<b>14</b>	The number of solution of the following equations $x_2 - x_3 = 1$ , $-x_1 + 2x_3 = -2$ , $x_1 - 2x_2 = 3$ is (a) Zero    (b) One    (c) Two    (d) Infinite		
<b>15</b>	If the system of linear equation $x + 2ay + az = 0$ , $x + 3by + bz = 0$ , $x + 4cy + cz = 0$ has a non zero solution, then $a, b, c$ (a) Are in A.P.    (b) Are in G. P. (c) Are in H. P.    (d) Satisfy $a + 2b + 3c = 0$		
<b>16</b>	The values of $x, y, z$ in order of the system of equations $3x + y + 2z = 3$ , $2x - 3y - z = -3$ , $x + 2y + z = 4$ , are (a) $2, 1, 5$ (b) $1, 1, 1$ (c) $1, -2, -1$ (d) $1, 2, -1$		
<b>17</b>	The system of equations $x_1 - x_2 + x_3 = 2$ , $3x_1 - x_2 + 2x_3 = -6$ and $3x_1 + x_2 + x_3 = -18$ has (a) No solution    (b) Exactly one solution (c) Infinite solutions    (d) None of these		
<b>18</b>	The number of values of $k$ for which the system of equations $(k + 1)x + 8y = 4k$ , $kx + (k + 3)y = 3k - 1$ has infinitely many solutions, is (a) $0$ (b) $1$ (c) $2$ (d) Infinite		

<p><b>19</b></p>	<p>Value of <math>\begin{vmatrix} x+y &amp; x &amp; x \\ 5x+4y &amp; 4x &amp; 2x \\ 10x+8y &amp; 8x &amp; 3x \end{vmatrix}</math> is:</p> <p>(a) 0                      (b) <math>x^3</math>                      (c) <math>y^3</math>                      (d) none of these</p>		
<p><b>20</b></p>	<p>Value of <math>\begin{vmatrix} 1! &amp; 2! &amp; 3! \\ 2! &amp; 3! &amp; 4! \\ 3! &amp; 4! &amp; 5! \end{vmatrix}</math> is:</p> <p>(a) 2                      (b) 6                      (c) 24                      (d) 120</p>		
<p><b>Case Study</b></p>			
<p>Area of a triangle whose vertices are <math>(x_1, y_1), (x_2, y_2)</math> and <math>(x_3, y_3)</math> is given by the determinant</p> $\Delta = \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$ <p>Since, area is a positive quantity, so we always take the absolute value of the determinant <math>\Delta</math>. Also, the area of the triangle formed by three collinear points is zero. Based on the above information, answer the following questions.</p>			

21	<p>Find the area of the triangle whose vertices are <math>(-2, 6)</math>, <math>(3, -6)</math> and <math>(1, 5)</math>.</p> <p>(a) 30 sq. units      (b) 35 sq. units      (c) 40 sq. units      (d) 15.5 sq. units</p>		
22	<p>If the points <math>(2, -3)</math>, <math>(k, -1)</math> and <math>(0, 4)</math> are collinear, then find the value of <math>4k</math>.</p> <p>(a) 4      (b) <math>\frac{7}{140}</math>      (c) 47      (d) <math>\frac{40}{7}</math></p>		
23	<p>If the area of a triangle <math>ABC</math>, with vertices <math>A(1, 3)</math>, <math>B(0, 0)</math> and <math>C(k, 0)</math> is 3 sq. units, then a value of <math>k</math> is</p> <p>(a) 2      (b) 3      (c) 4      (d) 5</p>		
24	<p>Using determinants, find the equation of the line joining the points <math>A(1, 2)</math> and <math>B(3, 6)</math>.</p> <p>(a) <math>y = 2x</math>      (b) <math>x = 3y</math>      (c) <math>y = x</math>      (d) <math>4x - y = 5</math></p>		
25	<p>If <math>A \equiv (11, 7)</math>, <math>B \equiv (5, 5)</math> and <math>C \equiv (-1, 3)</math>, then</p> <p>(a) <math>\triangle ABC</math> is scalene triangle      (b) <math>\triangle ABC</math> is equilateral triangle  (c) <math>A, B</math> and <math>C</math> are collinear      (d) None of these</p>		