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CLASS XI – MATHEMATICS

BINOMIAL THEOREM

| | | | | |
|---|--|-------------------------|-------------------------|--|
| 1 | The term independent of x in the expansion of $\left(\frac{x+1}{x^{2/3}-x^{1/3}+1} - \frac{x-1}{x-x^{1/2}}\right)$ is | | | |
| 4 | 120 | 210 | 310 | |
| 2 | Coefficient of x^{11} in the expansion of $(1+x^2)^4(1+x^3)^7(1+x^4)^{12}$ is | | | |
| 1051 | 1106 | 1113 | 1120 | |
| 3 | The sum of coefficients of integral powers of x in the expansion of $(1-2\sqrt{x})^{50}$ is | | | |
| $\frac{1}{2}(3^{50}+1)$ | $\frac{1}{2}(3^{50})$ | $\frac{1}{2}(3^{50}-1)$ | $\frac{1}{2}(2^{50}+1)$ | |
| 4 | If $C(n-1, r) = (K^2-3)C(n, r+1)$, then $K \in$ | | | |
| $(-\infty, 2]$ | $[2, \infty)$ | $(-\sqrt{3}, \sqrt{3})$ | $(\sqrt{3}, 2]$ | |
| 5 | $(C_0^{30})(C_{10}^{30}) - (C_1^{30})(C_{11}^{30}) + \dots + (C_{20}^{30})(C_{30}^{30}) =$ | | | |
| C_{11}^{30} | C_{10}^{60} | C_{10}^{30} | C_{55}^{65} | |
| 6 | Prove that the coefficient of x^6 in the expansion of $(1+4x^2+10x^4+20x^6)^{-\frac{3}{4}}$ is -1. | | | |
| 7 | Prove that : $\sqrt{8} = 1 + \frac{3}{4} + \frac{3}{4} \cdot \frac{5}{8} + \frac{3.5.7}{4.8.12} + \dots$ | | | |
| 8 | If the expansion of $(1+x+x^2)^n$ be $a_0 + a_1x + a_2x^2 + \dots + a_{2n}x^{2n}$, then show that $a_0 + a_3 + a_6 + \dots = a_1 + a_4 + a_7 + \dots = a_2 + a_5 + a_8 + \dots = 3^{n-1}$ | | | |
| 9 | Prove that approximately, when x is very small, then $\frac{3(x+\frac{4}{9})^{\frac{1}{2}}(1-\frac{3}{4}x^2)^{\frac{1}{3}}}{2(1+\frac{9}{16}x)^2} = 1 - \frac{307}{256}x^2$ | | | |
| 10 | If $C_0, C_1, C_2, \dots, C_n$ denotes the coefficients in the expansion of $(1+x)^n$, then prove that | | | |
| 1) $C_0 + \frac{C_1}{2} + \frac{C_2}{3} + \dots + \frac{C_n}{n+1} = \frac{2^{2n+1}-1}{n+1}$ | | | | |
| 2) $(C_0 + C_1)(C_1 + C_2) \dots (C_{n-1} + C_n) = \frac{C_0 C_1 C_2 \dots C_n (n+1)^n}{n!}$ | | | | |
| 3) $2C_0 + 2^2 \frac{C_1}{2} + 2^3 \frac{C_2}{3} + \dots + 2^{n+1} \frac{C_n}{n+1} = \frac{3^{n+1}-1}{n+1}$ | | | | |
| 4) $C_0 C_r + C_1 C_{r+1} + C_2 C_{r+2} + \dots + C_{n-r} C_n = \frac{2n!}{(n-r)!(n+r)!}$ | | | | |

PERMUTATION AND COMBINATION

| | | | | |
|-----------|---|------------------------|---------------------|------------------|
| 1 | The number of diagonals that can be formed by a polygon of 100 sides is | | | |
| | 4950 | 4850 | 5000 | 10000 |
| 2 | If out of $p + q + r$ things p are alike, q are alike and r are alike, then the number of arrangements equals | | | |
| | $\frac{(p + q + r)!}{p! q!}$ | $(p+1)(q+1)r-1$ | $2^{p+q} + 2^r - 1$ | $(p+q+1)(r+1)-1$ |
| 3 | Total number of 9 digit numbers which have all different digits | | | |
| | $10!$ | $9!$ | $9.9!$ | $10.10!$ |
| 4 | Total number of seven digit numbers, the sum of whose digits is even, is | | | |
| | 9000000 | 4500000 | 810000 | None of these |
| 5 | Out of 8 sailors on a boat, 3 can work only on one side and 2 can only on the other side. The number of ways the sailors can be arranged on the boat is | | | |
| | 1700 | 1720 | 1728 | 1736 |
| 6 | A set contains $(2n+1)$ elements. If the number of subsets of this set which contain atmost n elements is 4096, then the value of n is | | | |
| | 6 | 15 | 21 | None of these |
| 7 | The number of numbers between 1 to 10^{10} which contain the digit 1 is | | | |
| | 9^{10} | $10^{10} - 9^{10} - 1$ | $10^{10} - 9^{10}$ | None of these |
| 8 | The number of positive integers which can be formed by using each digit not more than once in each number is | | | |
| | 1200 | 1500 | 1600 | 1630 |
| 9 | Passengers are to travel by a double decked bus which can accommodate 13 in upper deck and 7 in lower deck. The number of ways that they can be distributed if 5 refuse to sit in the upper deck and 8 refuse to sit in the lower deck is | | | |
| | 25 | 21 | 18 | 15 |
| 10 | There are $(n+1)$ white balls and $(n+1)$ black balls each set number 1 to $n+1$. The number of ways the balls can be arranged in a row so that the adjacent balls are of different colours, is | | | |
| | $[(n + 1)!]^2$ | $2(2n)!$ | $2[(n + 1)!]$ | $2[(n + 1)!]^2$ |