

SAMPLE PAPER - 2014
MATHEMATICS
Class – XII

MAXIMUM MARKS:100

TIME: 3 HOURS.

General Instructions:

- All questions are compulsory.
- The questions paper consists of 26 questions divided into three sections A,B and C. Section A comprises of 06 questions of one mark each, section B comprises of 13 questions of four marks each and section C comprises of 7 questions of six marks each.
- All questions in Section A are to be answered in one word, one sentence or as per the exact requirement of the question.
- There is no overall choice. However, internal choice has been provided in 4 questions of four marks each and 2 questions of six marks each. You have to attempt only one of the alternatives in all such questions.
- Use of calculators is not permitted. You may ask for logarithmic tables, if required.

SECTION – A

- 1) If $\begin{pmatrix} x-y & z \\ 2x-y & w \end{pmatrix} = \begin{pmatrix} -1 & 4 \\ 0 & 5 \end{pmatrix}$, find the value of x, y, z and w.
- 2) If $f(x) = \frac{4x+3}{6x-4}$, find $f \circ f(x)$
- 3) Find the principal value of $\tan^{-1}(-1)$.
- 4) The total revenue in Rupees received from the sale of x units of a product is given by $R(x) = 3x^2 + 36x + 5$. Find the marginal revenue, when $x=5$, where by marginal revenue we mean the rate of change of total revenue with respect to the number of items sold at an instant.
- 5) Evaluate $\int e^x \left(\frac{1}{1+x^2} + \tan^{-1} x \right) dx$.
- 6) If A is a square matrix of order 3 such that $|\text{adj } A| = 36$ find $|A|$

SECTION- B

- 7) Show that the relation R in set $A = \{ x \in \mathbb{Z}, 0 \leq x \leq 12 \}$ given by $R = \{(a,b): |a-b| \text{ is a multiple of } 4\}$ is an equivalence relation.
- 8) Find the values of a and b such that the function defined by $f(x) \begin{cases} 5, & \text{if } x \leq 2 \\ ax+b, & \text{if } 2 < x < 10 \\ 21, & \text{if } x \geq 10 \end{cases}$ is continuous.

- 9) If $x = a(\cos \theta + \theta \sin \theta)$, $y = a(\sin \theta - \theta \cos \theta)$ find $\frac{d^2y}{dx^2}$.
- 10) Differentiate $\sin^2 \left[\cot^{-1} \left(\sqrt{\frac{1+x}{1-x}} \right) \right]$ w.r.t. x . OR. Differentiate $(\log x)^x + (x)^{\log x}$ w.r.t. x .
- 11) Find a point on the curve $y = x^3 - 2x$, where the tangent is parallel to the chord joining $(1, -2)$ and $(2, 2)$.
- 12) Find the intervals in which $-2x^3 - 9x^2 - 12x + 1$ is increasing or decreasing.
- 13) Evaluate $\int \frac{\cos x}{(1 - \sin x)(2 - \sin x)} dx$ OR . Evaluate $\int \frac{e^x}{\sqrt{5 - 4e^x - e^{2x}}} dx$
- 14) Evaluate $\int \frac{dx}{\cos(x-a)\cos(x-b)}$ dx
- 15) Solve for x , $\sin^{-1} x + \sin^{-1} 2x = \frac{\pi}{3}$

OR

Prove $\sin^{-1} \frac{12}{13} + \cos^{-1} \frac{4}{5} + \tan^{-1} \frac{63}{16} = \pi$

- 16) Find the matrix p satisfying the matrix equation

$$\begin{bmatrix} 2 & 1 \\ 3 & 2 \end{bmatrix} p \begin{bmatrix} -3 & 2 \\ 5 & -3 \end{bmatrix} = \begin{bmatrix} 1 & 2 \\ 2 & -1 \end{bmatrix}.$$

- 17) Test for bijective for that the function $f: R \rightarrow R$, given by

$$f(x) = f(x) = \begin{cases} 1 & \text{if } x > 0 \\ 0, & \text{if } x = 0 \\ -1 & \text{if } x < 0 \end{cases}$$

OR

$f: R \rightarrow [4, \infty]$ given by $f(x) = x^2 + 4$, Show that f is invertible with the inverse f^{-1} of f given by $f^{-1}(y) = \sqrt{y - 4}$

- 18) Test the differentiability $|x - 3|$.
- 19) Find the approximate value of $\sqrt[3]{(0.037)}$ using differentiation.

SECTION - C

- 20) Using properties of determinants show that $\begin{vmatrix} 1+a & 1 & 1 \\ 1 & 1+b & 1 \\ 1 & 1 & 1+c \end{vmatrix} = abc + bc + ca + ab$.
- 21) Evaluate $\int \sin^{-1} \sqrt{\frac{x}{a+x}} dx$

22) Find BA where $A = \begin{pmatrix} 1 & -1 & 0 \\ 2 & 3 & 4 \\ 0 & 1 & 2 \end{pmatrix}$, $B = \begin{pmatrix} 2 & 2 & -4 \\ -4 & 2 & -4 \\ 2 & -1 & 5 \end{pmatrix}$. Using the result

Solve: $x - y = 3$; $2x + 3y + 4z = 17$; $y + 2z = 7$.

OR

Using elementary transformation find the inverse of the matrix $\begin{bmatrix} 1 & 3 & -2 \\ -3 & 0 & -5 \\ 2 & 5 & 0 \end{bmatrix}$

23) A window is in the form of a rectangle surmounted by a semi-circular opening. The total perimeter of the window is 10m. Find the dimensions of the window to admit maximum light through the whole opening.

OR

A point on the hypotenuse of a right triangle is at a distances a and b from the sides of the triangle .Show that the minimum length of the hypotenuse is $\left(a^{\frac{2}{3}} + b^{\frac{2}{3}}\right)^{\frac{3}{2}}$.

24). $\int \frac{x^2+1}{x^4+x^2+1} dx$

25) It is given that for the function & given by $f(x)=x^3 + bx^2+ax$, $x \in [1,3]$, Rolle's theorem hold with $C=2+\frac{1}{\sqrt{3}}$. Find the value of a & b

26) Find the equation of tangents to the curve $y=4x^3-2x^5$, at the point where the tangent passes through origin.
